Event history models

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Political science is full of phenomena that involve time

- unemployment, cabinets (governments), war, peace, negotiations...
- they contain two components:
 - an event (a binary outcome)
 - a duration (a "spell")

 \Rightarrow glass half full/half empty situation

Class half-full? Or empty?

opportunity: duration may be a substantive measure of its own
e.g. ability for a cabinet to stay in office

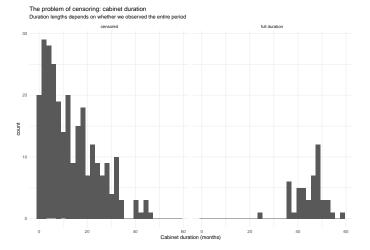
 constraint: observations are censored (i.e. we don't know when the spell ends)

- we can't truncate them (code them with max observed length): bias the slope (β)
- we can't remove them: bias the sample

 \Rightarrow model them as such

Censoring: two sets of observations

Censoring means that we don't observe the entire length of some spells



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Event history models

Choices and priorities

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Event history models require us to make quite a few choices

- information leveraged in the outcome (event/duration)
- unit of analysis (spell, spell + change in x, TSCS)
 - ▶ as a consequence: the nesting/correlation between repeated measures
- functional form (survival or hazard; parametric/estimated or semi-parametric/empirical)
- ties what to do when many observations experience the same event?

Data structures: unit of analysis

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Event history models often end up with complicated data structures and a host of "dependent" variables

- division between continuous time models and discrete time models is blurry
- unit of analysis:
 - spell-level: as simple as it gets (duration + event/no event)
 - spell-level + time varying covariates
 - fixed time period

 \Rightarrow Think ahead, because you will be doing data-wrangling

Spell-level: focus on duration

We can set up a data set with one observation == one duration/spell.

two outcomes:

- duration: how long governments stay in power
- censoring: all cabinets will end, but we don't always observe it (censor == 1).
- covariates: don't change during the spell

##		duration	censor12
##	1	7	1
##	2	27	1
##	3	6	1
##	4	49	0
##	5	7	1
##	6	3	1

Time-varying covariates: focus on time

If we want to include time-varying predictors, we need to make a new observation for each change in x (and not only in y)

- we "slice" up the duration for each unit
- **four dependent variables** to account for the nesting:
 - ► start and stop times (i.e. duration/counter) → focus of duration models
 - ▶ occurence of **event** (i.e. censoring) \rightarrow focus of BTSCS (e.g. logits)
 - id for each spell that is now "sliced up"
- this requires more controls for nesting (i.e. hierarchical models)

Data structures: unit of analysis

Time-series cross-section/panel

Same as panel data

- a fixed period for all units i.e. all units are observed at fixed time intervals (day, week year...)
- event(s) are reported (close friend of the poisson!)

Outcome leveraged

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We have potentially two outcomes

##		duration	censor12	
##	1	7	1	
##	2	27	1	
##	3	6	1	
##	4	49	0	
##	5	7	1	
##	6	3	1	

Focus on :

- event and control for duration: BTSCS approach
- duration (spell) punctuated by events: duration models
 - survival
 - failure

Event: Between-Time-Series-Cross-Section (BTSCS)

Event: Between-Time-Series-Cross-Section (BTSCS)

With panel data where the event is indicated, we may simply...

- regress the binary event on predictors of choice (logit, probit, log-log)
- control for the duration:
 - fixed effects for each duration (problem if we have low ratio event/no event)
 - "splines" (moving averages; hard to know what goes on)
 - cubic term
 - linear (!)

 \Rightarrow ignore/treat as noise the censoring and the time between events

Outcome leveraged Both: Duration models

Both: Duration models

Different focus in outcomes

Duration models draw information from both duration and event:

- explicit assumption that duration is partially unobserved.
- censored observations contribute with information about duration, but not event

Functional forms (duration)

Functional forms (duration)

Functional forms (duration)

Duration models assume a baseline probability that an event will occur that vary over time

- accelerated failure time (AFTs)
 - survival function
 - S(t) = 1 F(t) = Pr(T > t)
 - probability that observation has lasted until now

proportional hazard

- hazard function
- ▶ $h(t) = \frac{f(t)}{S(t)} = \frac{f(t)}{1 F(t)}$
- probability that the observation will experience the event, given that it has lasted until now

 \Rightarrow Same regression coefficients, but reverted (+/-)

Functional forms (duration) Proportional hazards

Proportional hazards

Proportional hazards

The outcome is hazard rates $h_i(t)$

- the proportion of observations that experience event in a given period
- among those that entered the period without having experienced the event

Hazards are proportional to the β

 $h_i(t) = h_o(t) exp(x_i^T \beta)$

h_o(t) baseline hazard varies over time:

- constant
- increasing/decreasing
- empirically determined

• $exp(x_i^T\beta)$ single set of slope coefficients

- proportional to (i.e. multiplicative) the baseline hazard
- $exp(\beta)$ reports the marginal change
 - positive β: increase in hazard/probability of event in period (decrease in duration)
 - negative β: decrase in hazard/probability of event in period (increase in duratoin)

 \Rightarrow Assumption that coefficients are constant across time

Two types of models

There are two estimation strategies/models

parametric models

- duration is continuous
- parameters determine the shape of the baseline hazard
- e.g. Weibull, exponential . . .

semi-parametric model

- duration is ordinal
- Cox proportional hazard

Cox proportional hazard models

Cox proportional hazard models

order data according to event date

- main asset: agnostic about functional form
- "partial likelihood":
 - within first date (period):
 - compare events to no-events
 - remove observations with events from data
 - within second date (period):
 - rinse and repeat
 - main weakness: ties
 - observations with the same event time
 - options for ordering/simulation (Efron, Breslow, exact)

Two assumptions to test in duration models

- proportional hazard: are coefficients the same over time
 - parametric and semi-parametric models
- functional form (parametric models)
- ties (Cox proportional hazard)

Dependencies between observations

Dependencies between observations

Dependencies between observations

Observations are often not independent from each other in these models

- risk set a duration for a natural unit is sliced up
- repeated events
- **Time dependency** (i.e. dates)
- different populations split-population data

Hierarchical data structures

Different vocabularies, same thing

- strata / fixed-effects (+ clustering of errors)
- frailty / random effects
- split population / zero-inflated models

Split population model

**We model two outcomes in two equations

- the "at-risk" group the probability of an event occurring at any given time for those who have not yet experienced the event
- the "affected" group the probability of an event occurring at any given time for those who have already experienced the event.